

Bounded Verification of Petri Nets and EOSs using Telingo: an Experience Report



Francesco Di Cosmo

Free University of Bozen-Bolzano

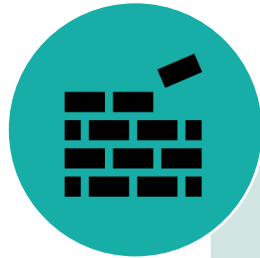
CILC 2024 - Rome, 28/6/2024



Tephilla Prince

IIT Dharwad, India

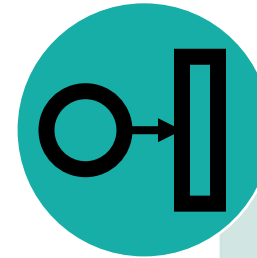
Contribution



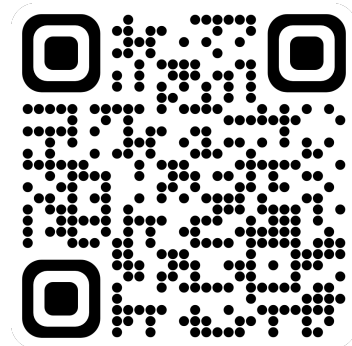
Created a
Verification
Prototype



For safety,
reach, cover,
deadlock

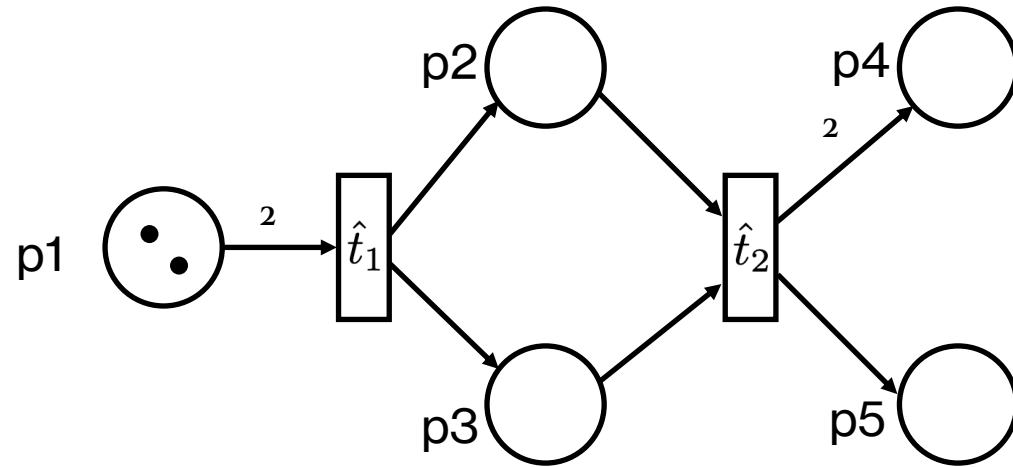
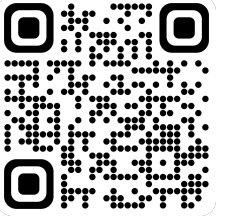


Of lossy PNs
and EOSs

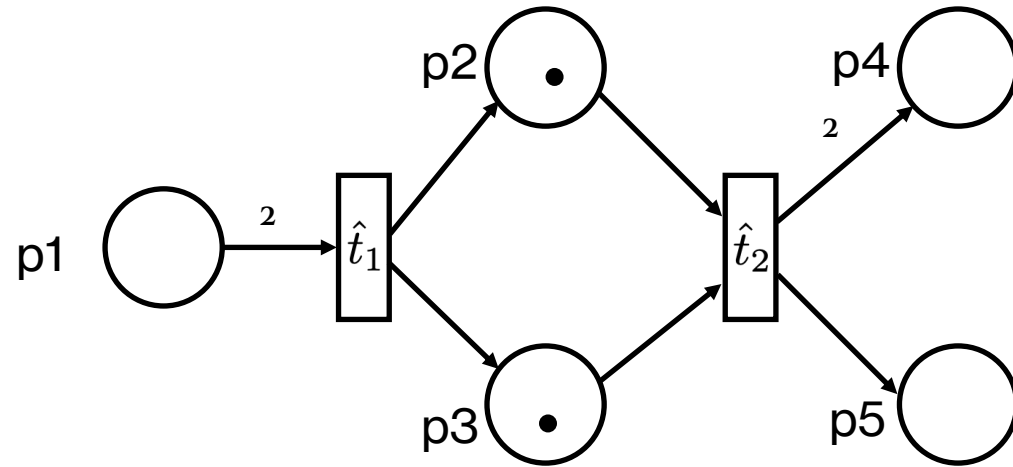
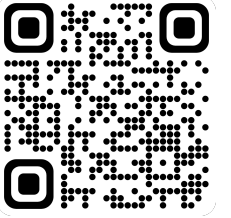


Available on
Zenodo

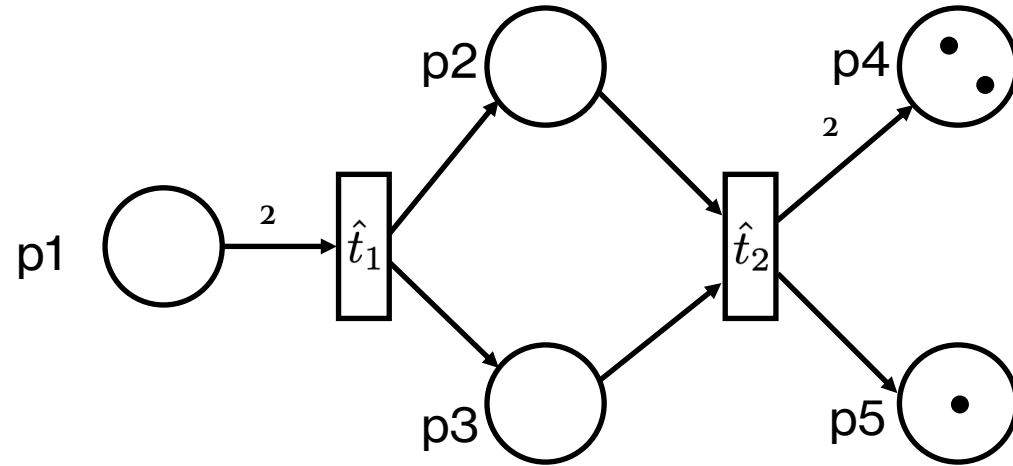
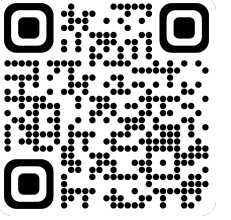
Petri Nets



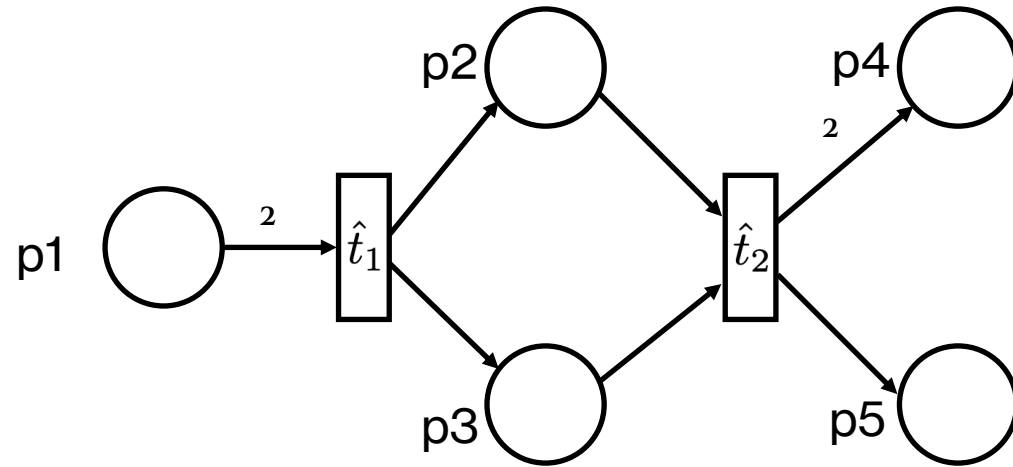
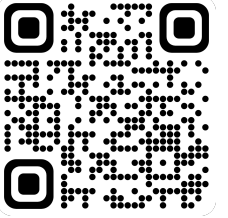
Petri Nets



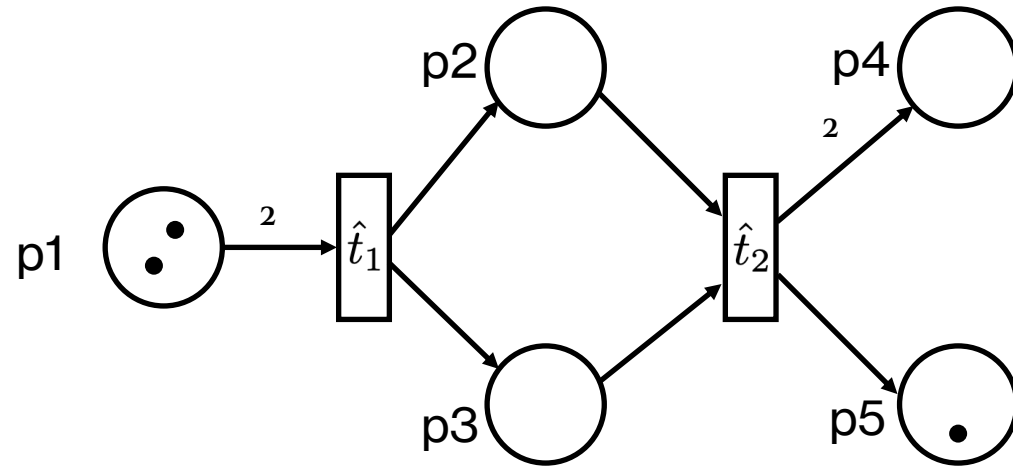
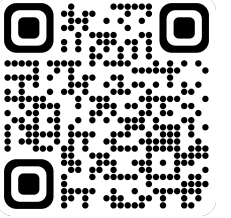
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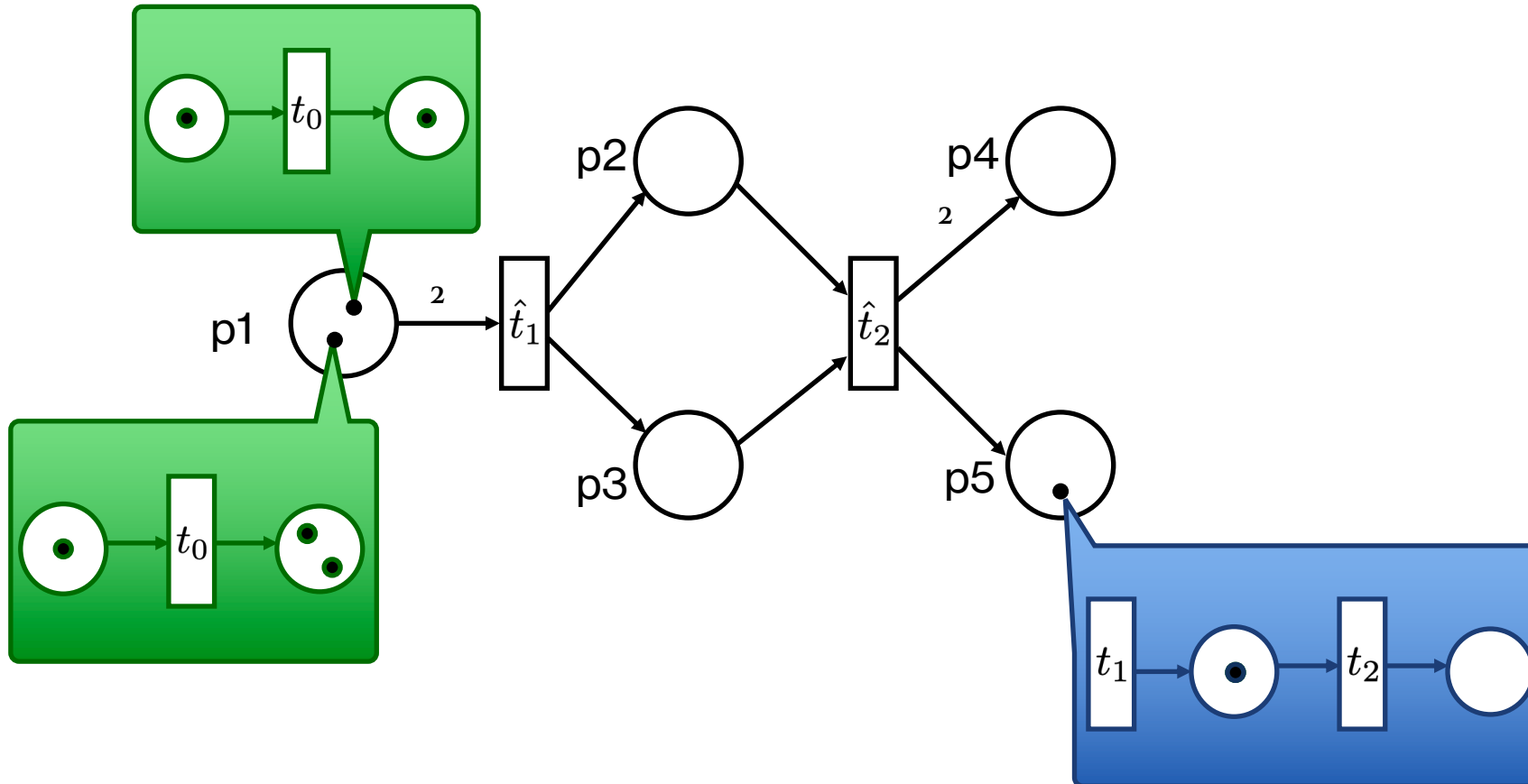
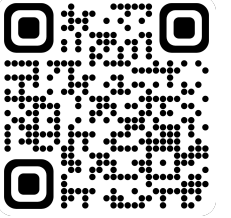
EOS – System Net



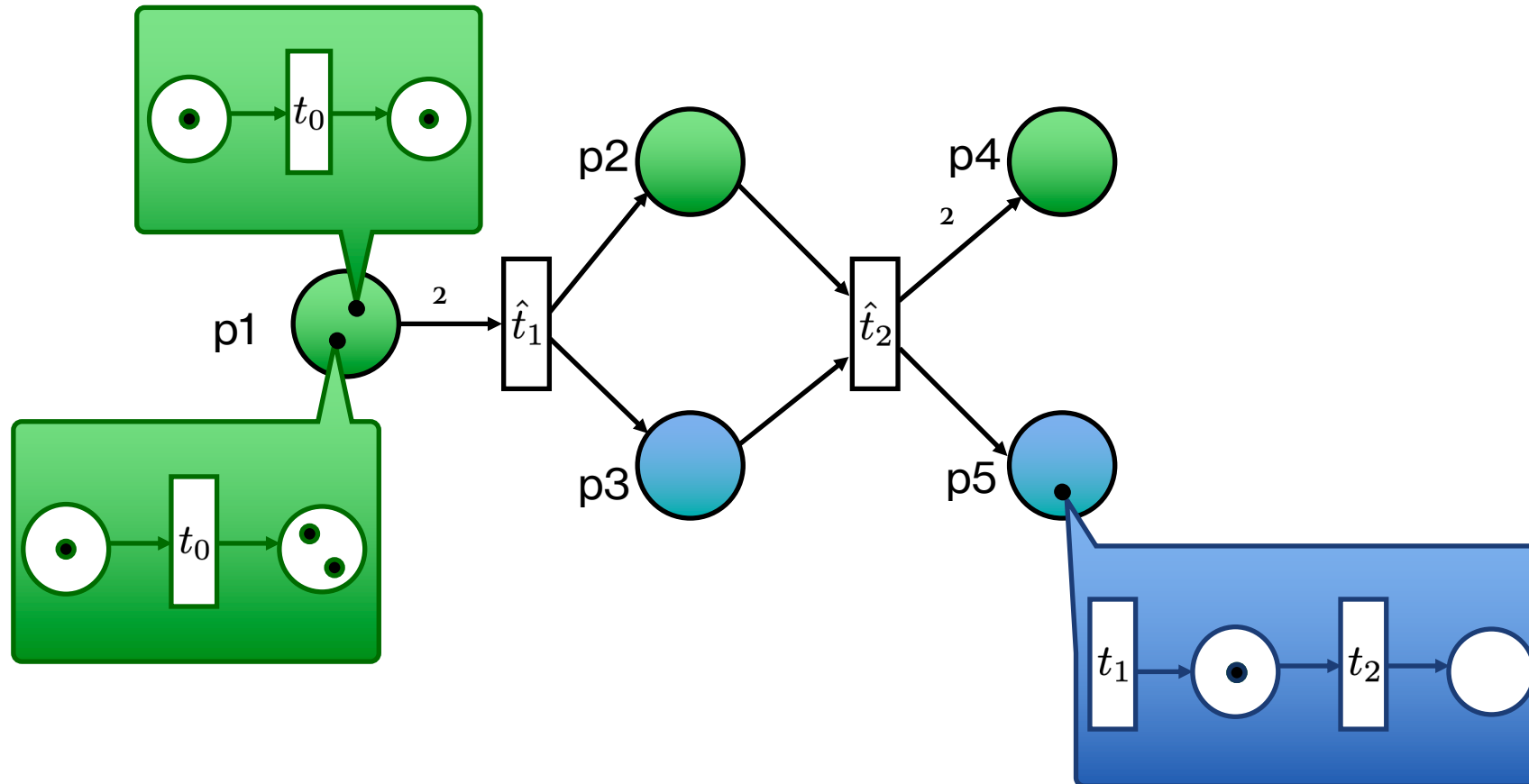
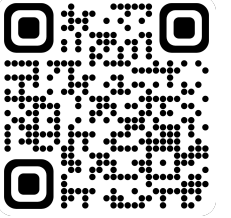
EOS – nested markings



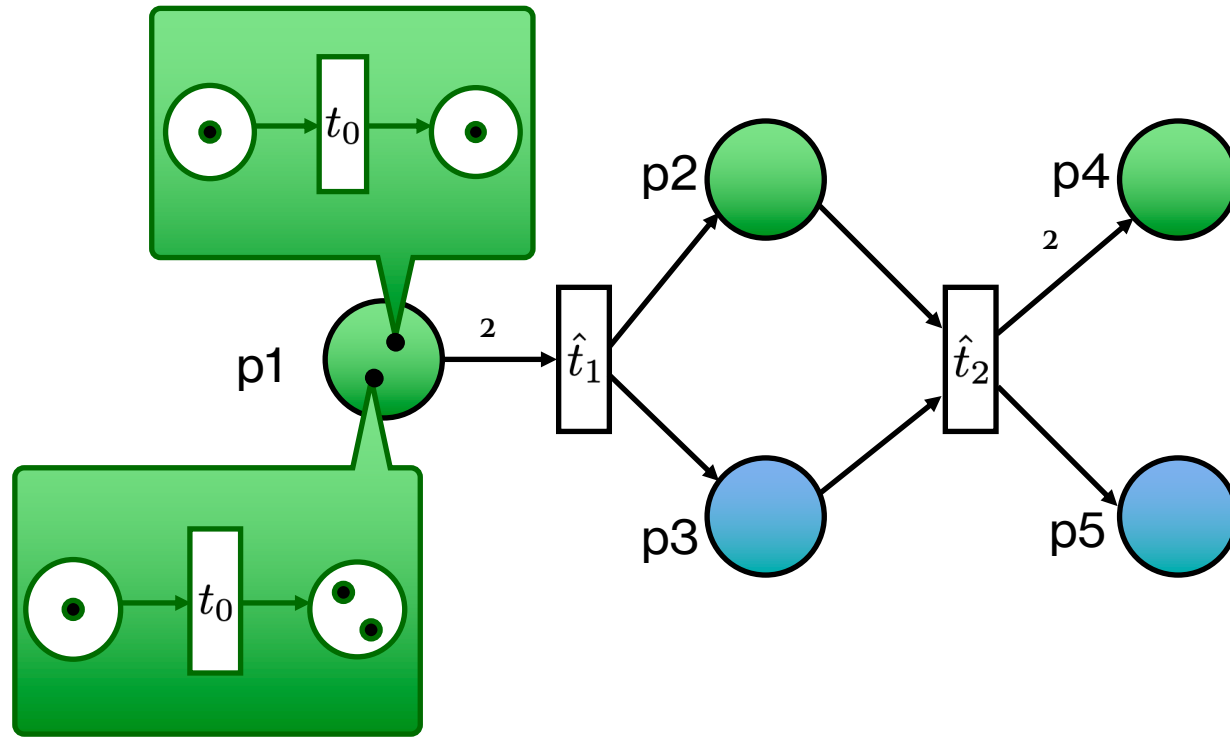
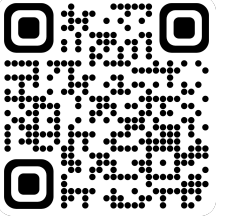
EOS – nested markings



EOS – typed places



EOS – object autonomous events



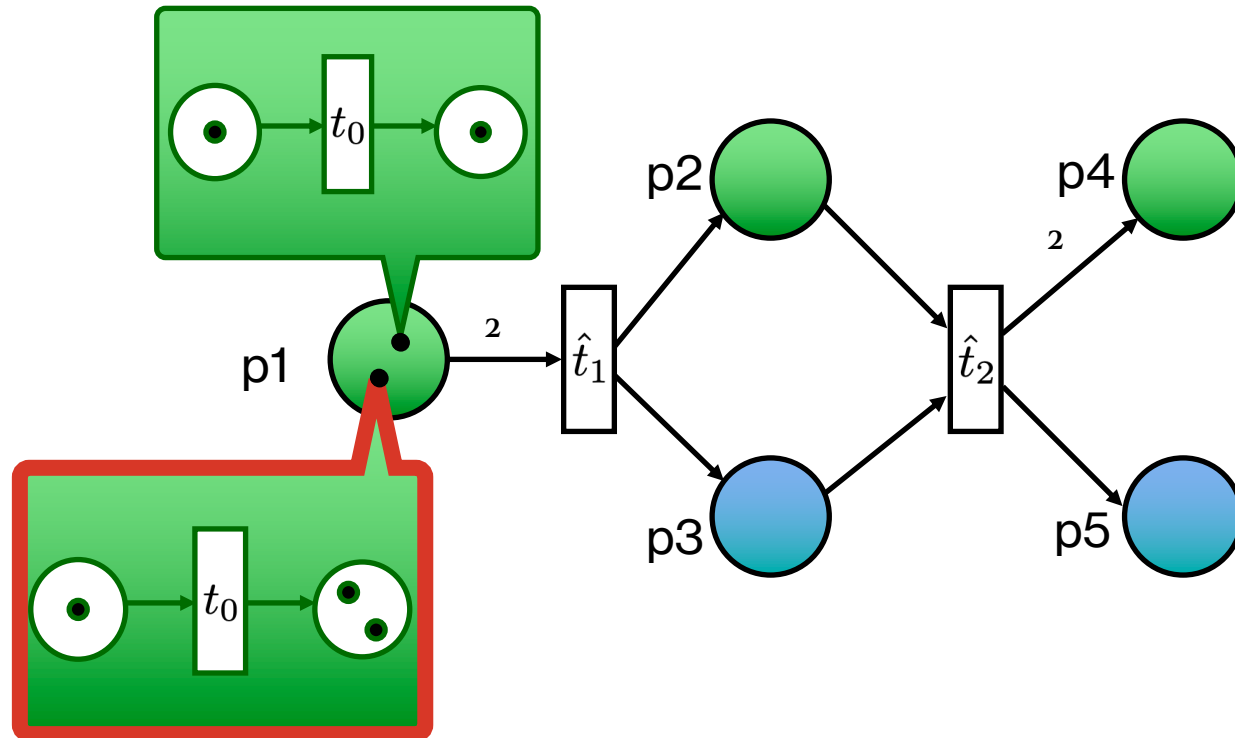
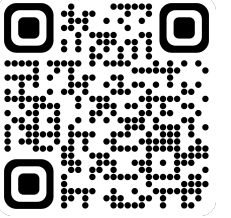
EVENTS

$$e_1 = (id_{p_1}, t_0)$$

$$e_2 = (\hat{t}_1, \emptyset)$$

$$e_3 = (\hat{t}_2, t_0 t_1 t_1)$$

EOS – object autonomous events



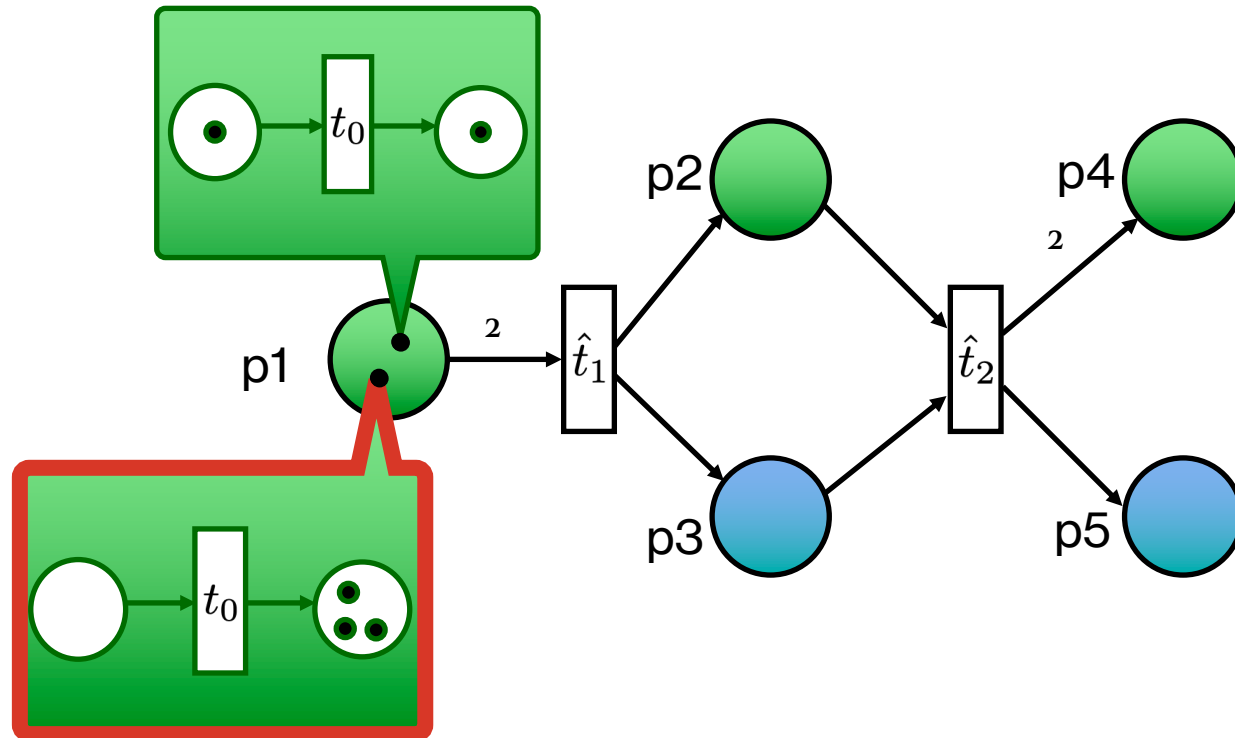
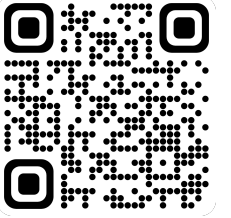
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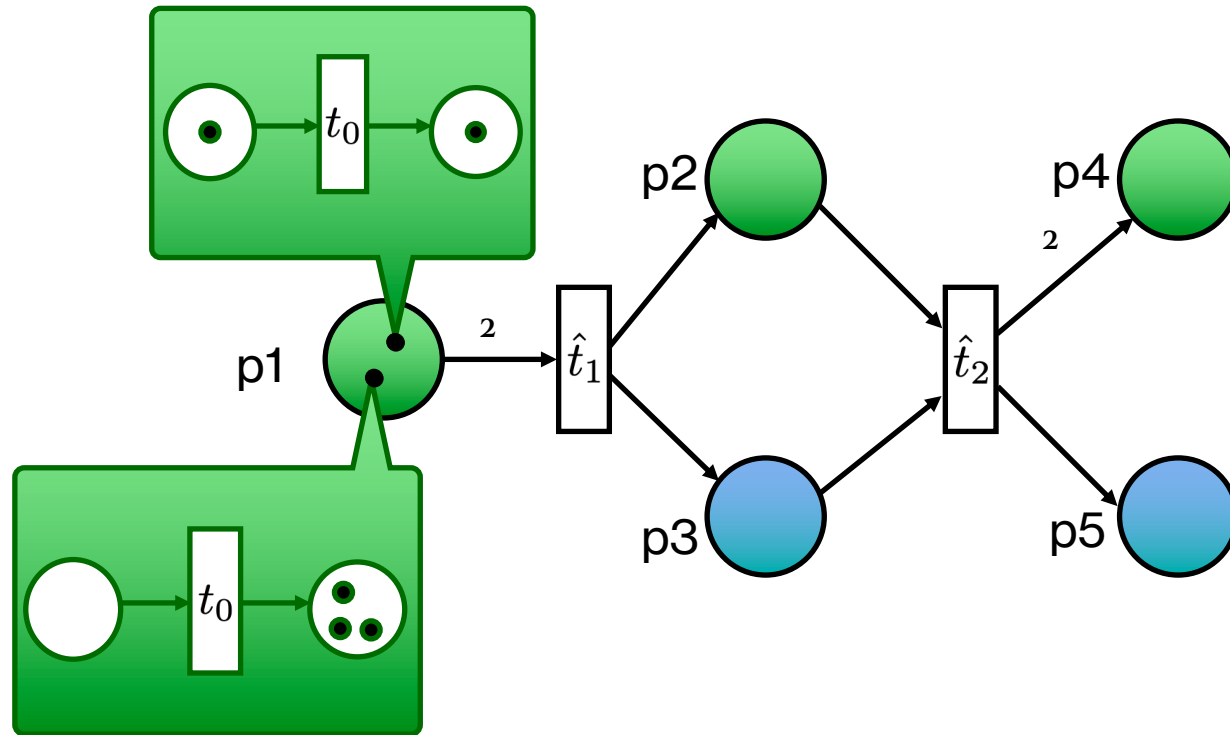
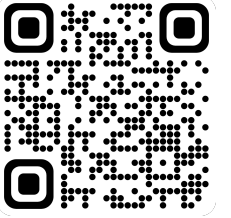
EOS – object autonomous events



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EOS – system autonomous events



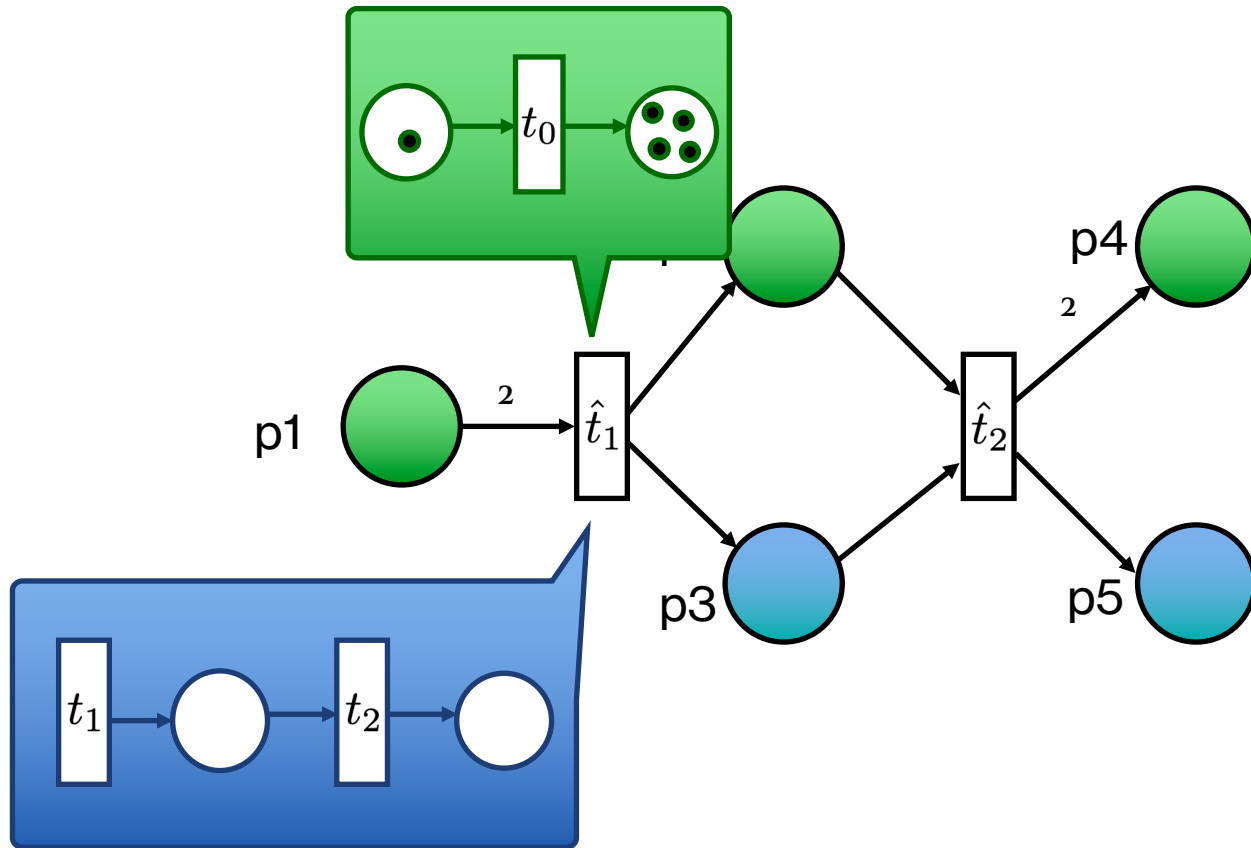
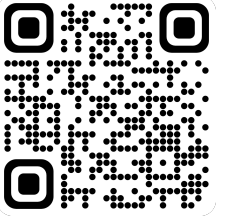
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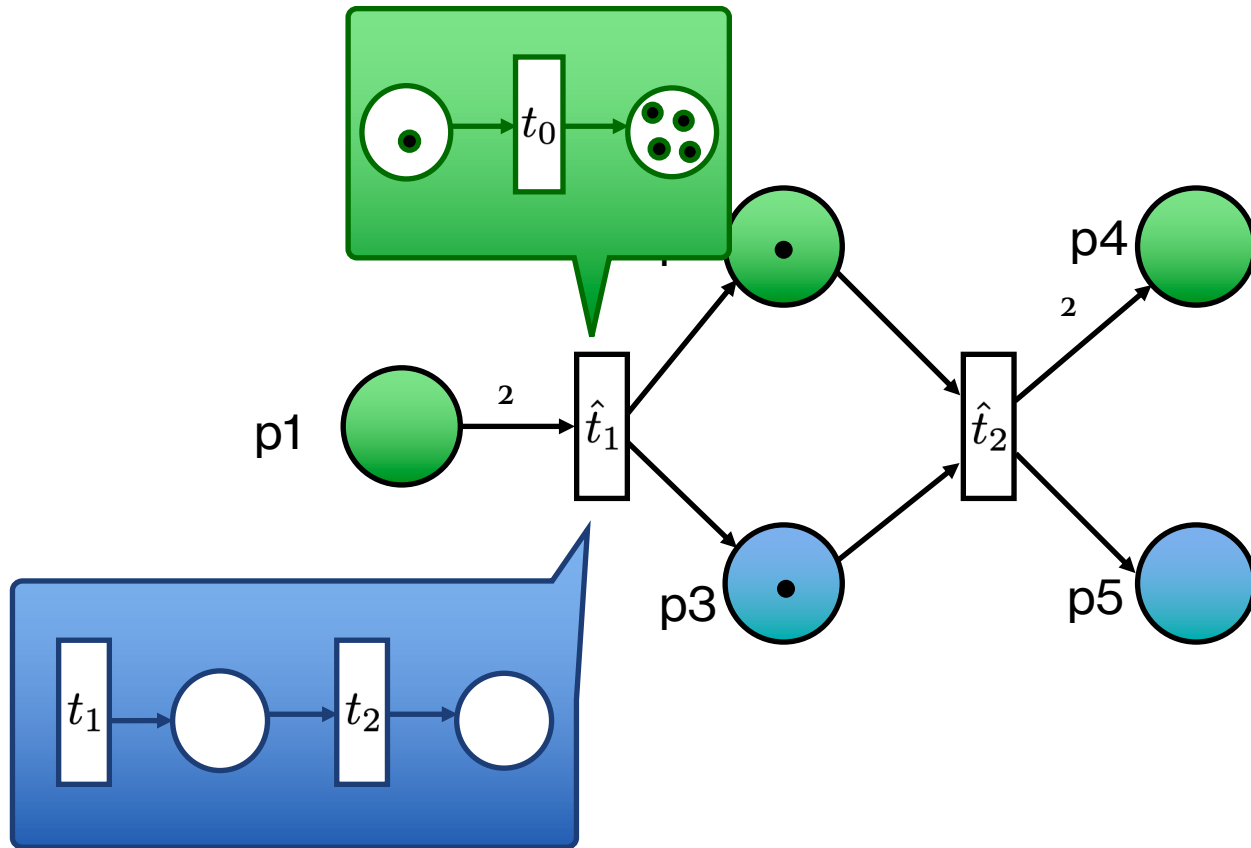
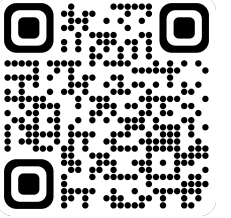
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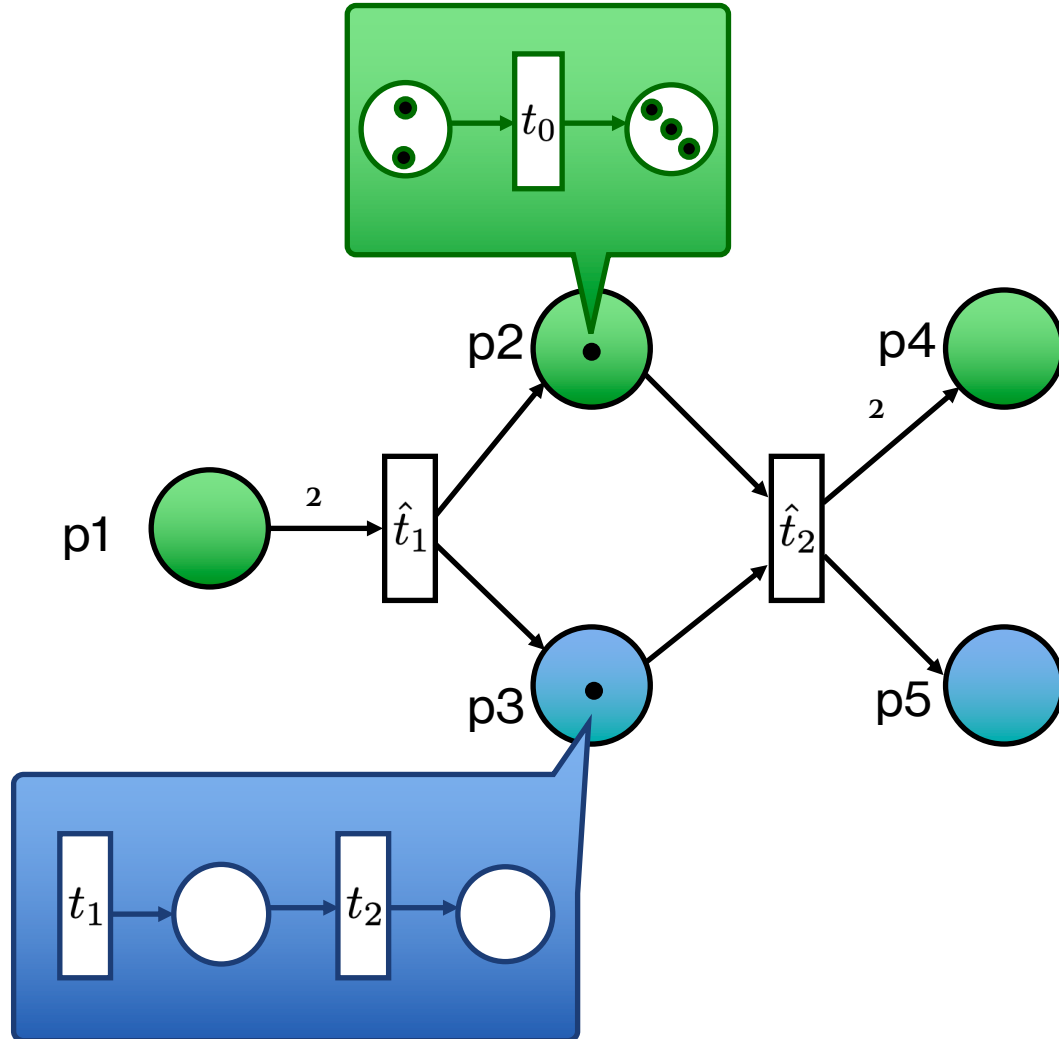
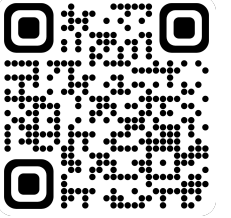
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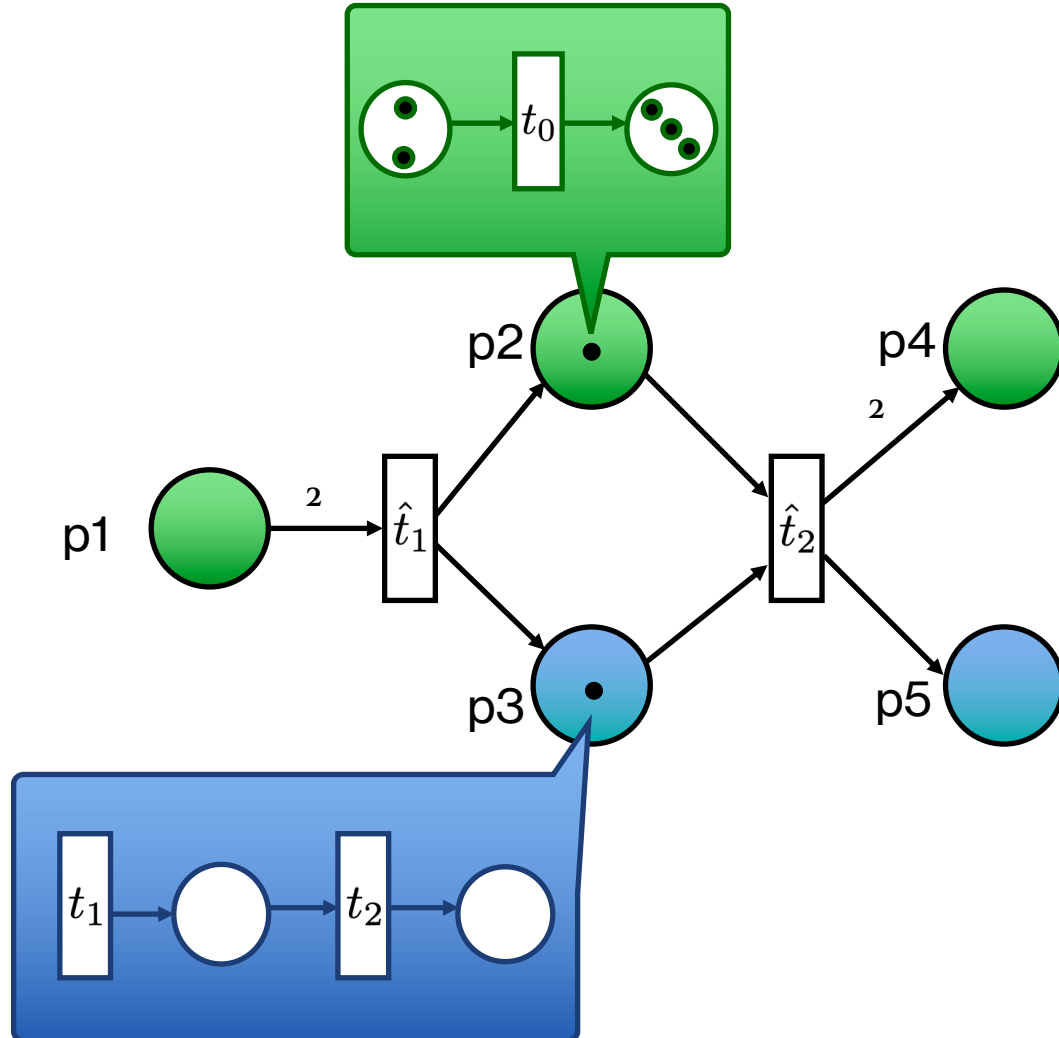
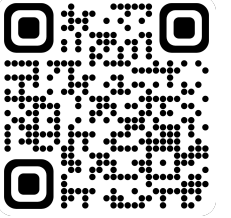
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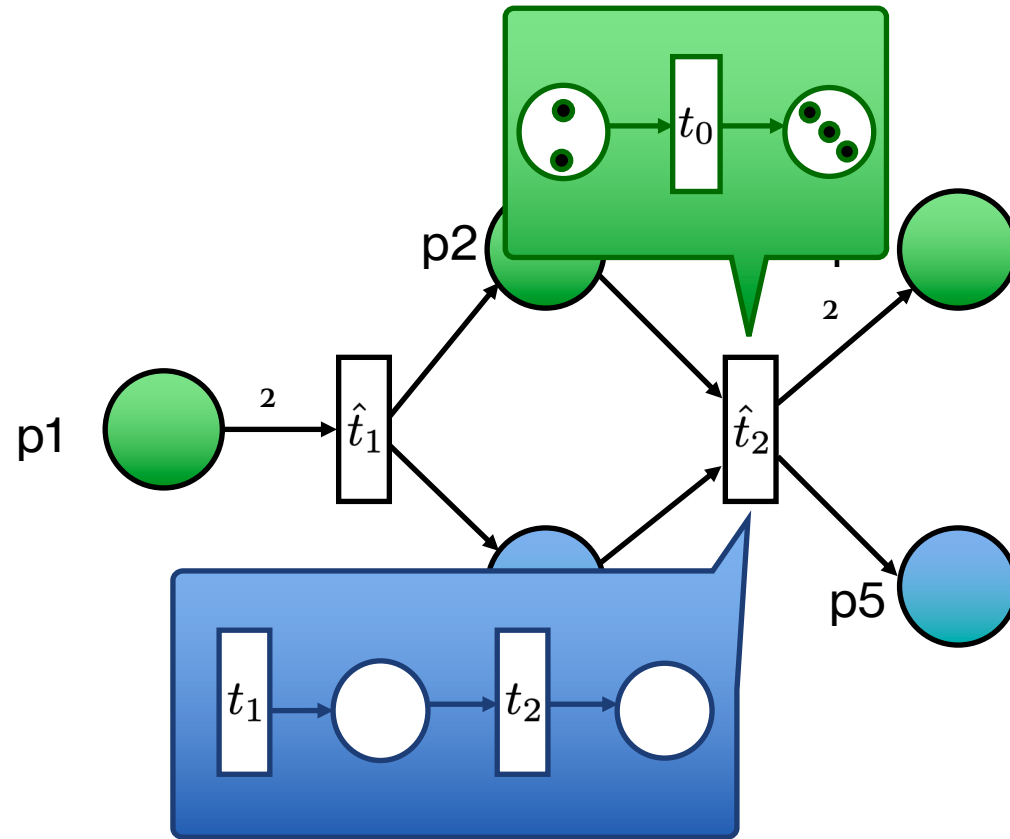
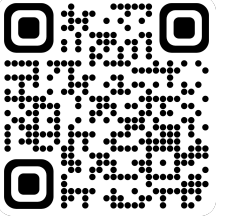
EOS – synchronization events



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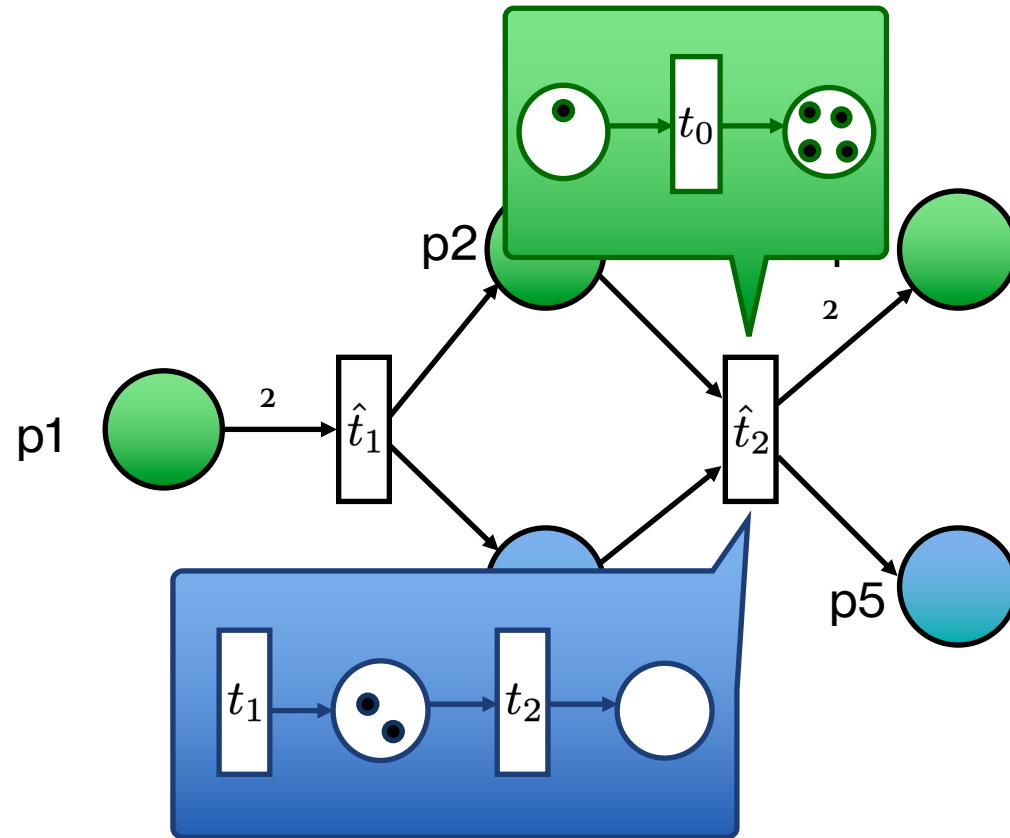
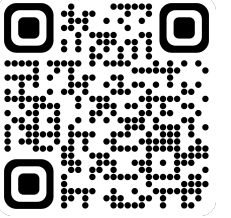
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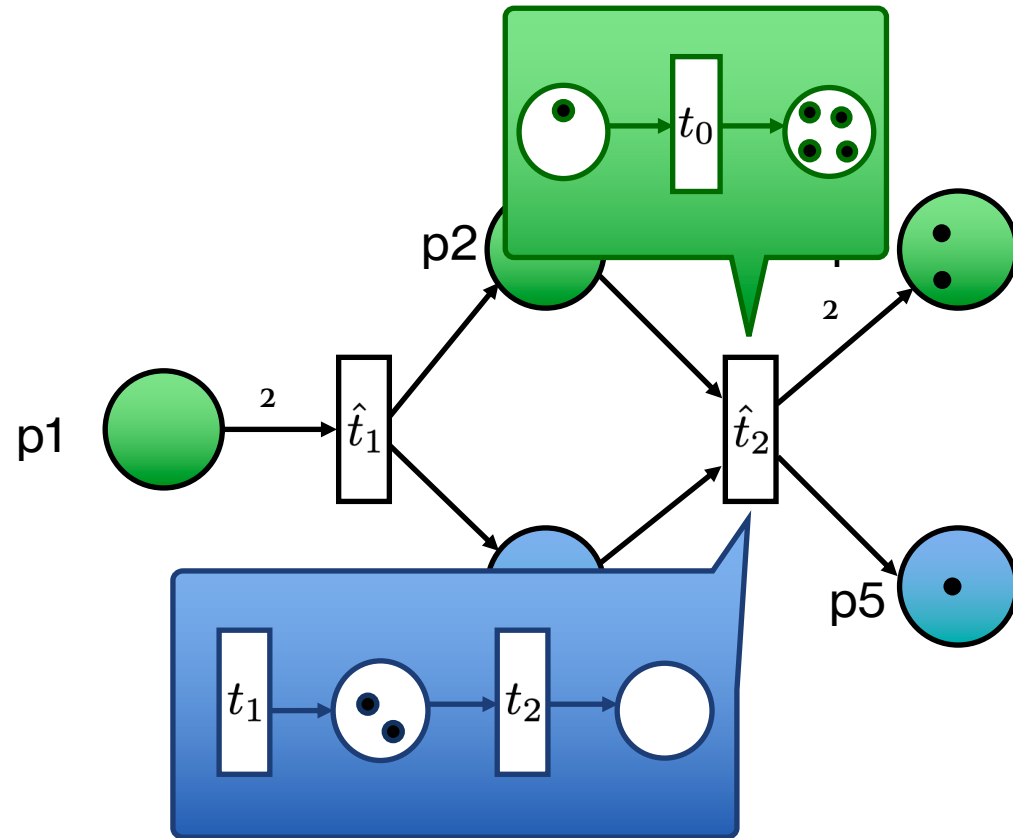
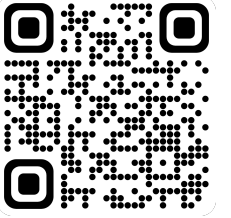
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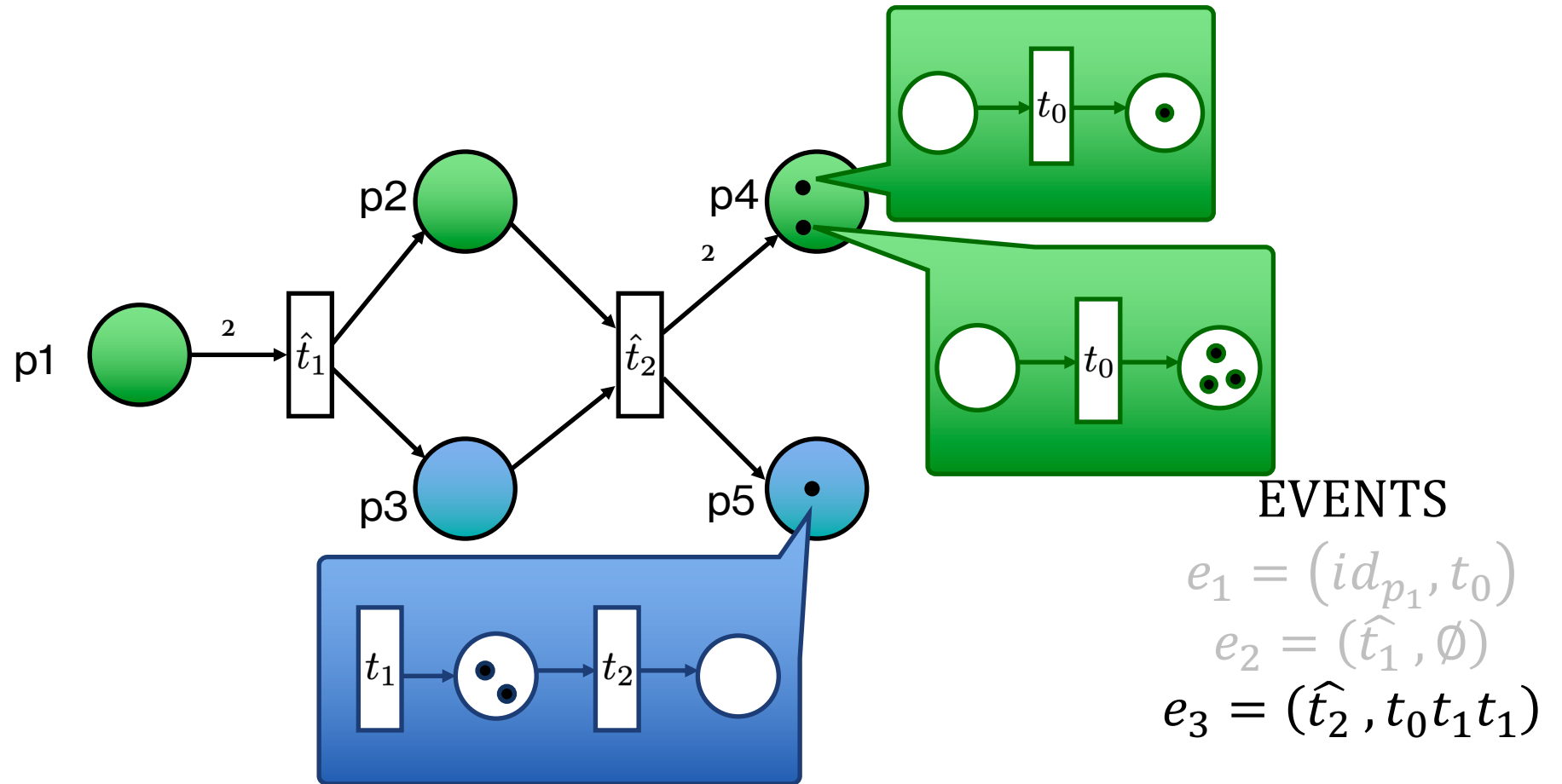
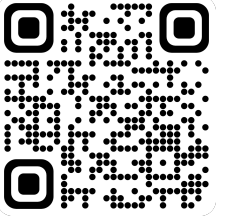
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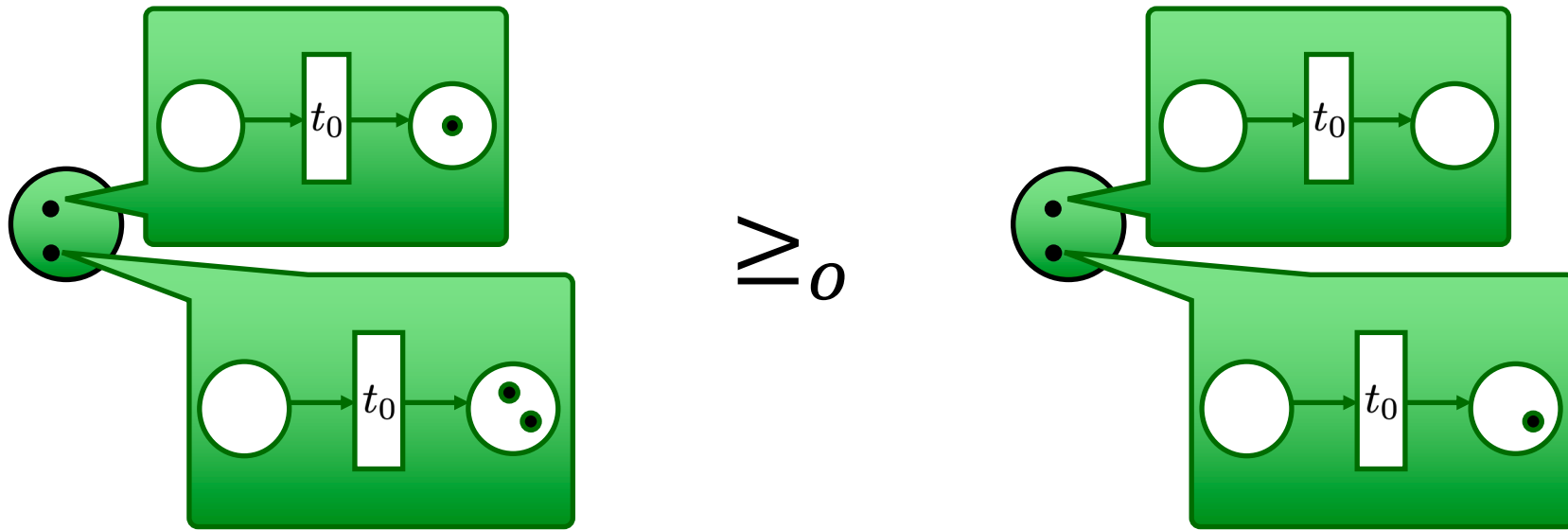
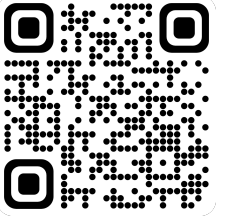
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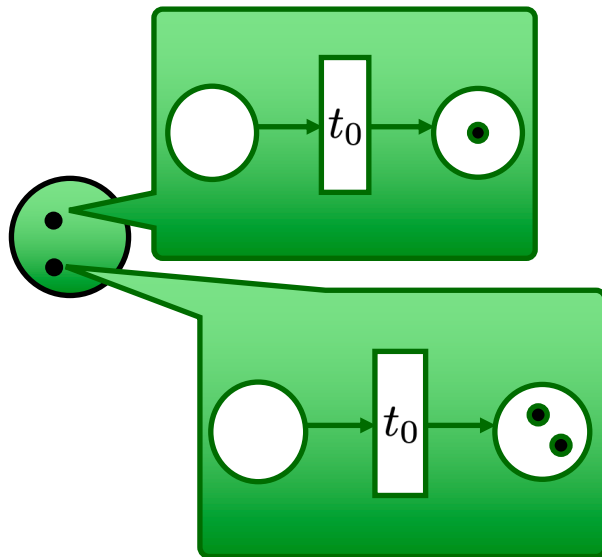
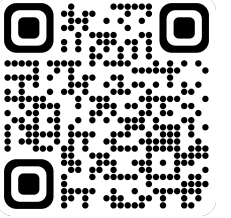
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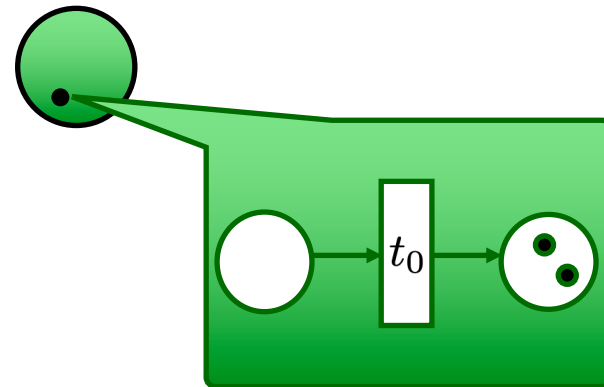
Object lossiness



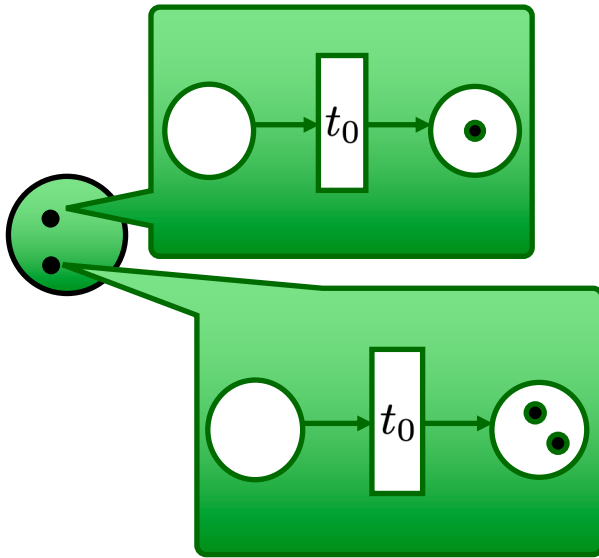
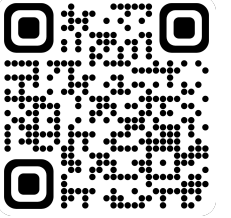
System lossiness



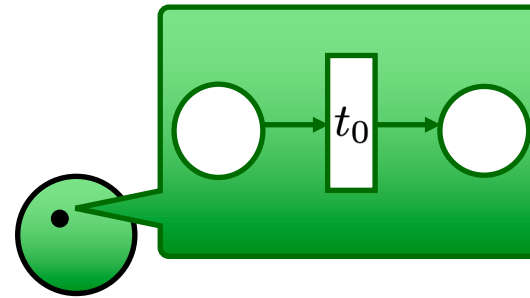
\mathbb{N}_s

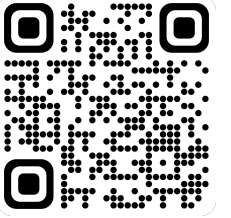


Full lossiness



\cong_f

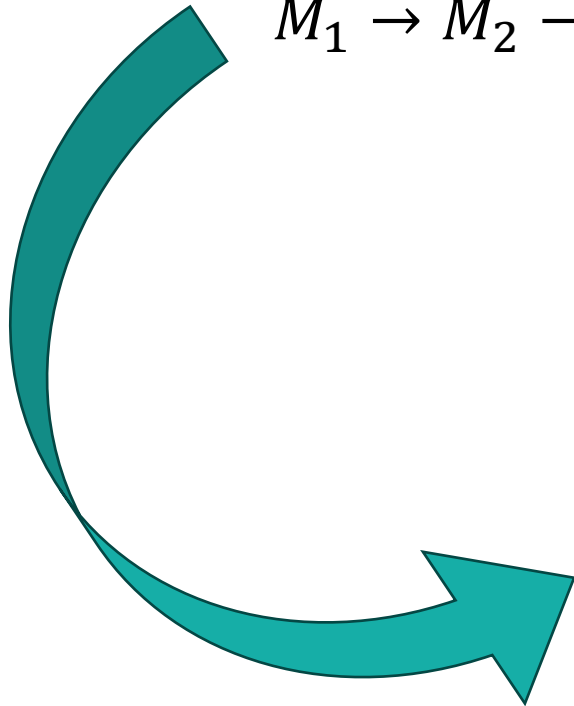




(\preceq, ℓ) -lossy runs

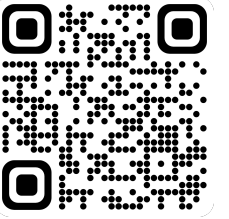
Perfect runs: only standard steps

$M_1 \rightarrow M_2 \rightarrow M_3 \rightarrow \dots$



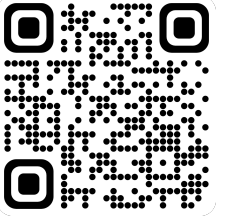
(\preceq, ℓ) -runs: at most $\ell \leq |\mathbb{N}|$ steps of type \preceq

$M_1 \rightarrow M_2 \succcurlyeq M'_3 \rightarrow M'_4 \succcurlyeq M'_5 \succcurlyeq M'_6 \rightarrow M_7 \rightarrow \dots$



(\preceq, ℓ) -lossy problems

Is the system **robust** up to ℓ occurrences of \preceq ?



(\preceq, ℓ) -lossy problems

Is the system **robust** up to ℓ occurrences of \preceq ?

(\preceq, ℓ) -deadlock freeness

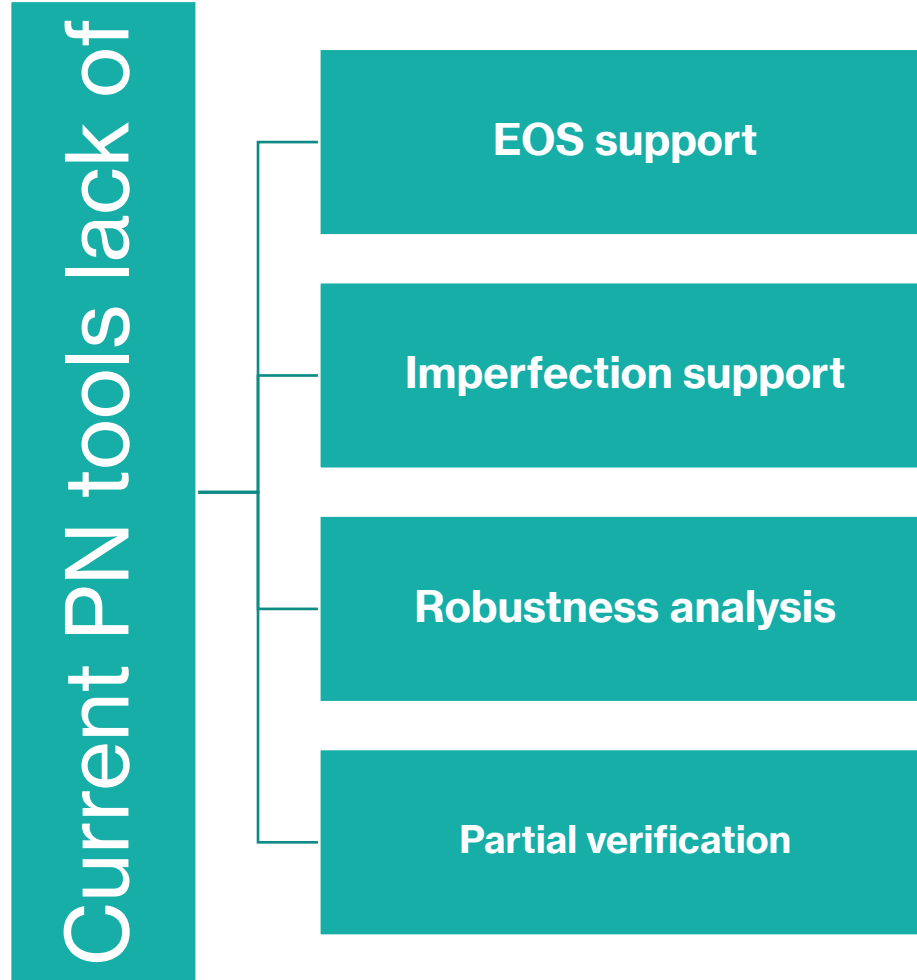
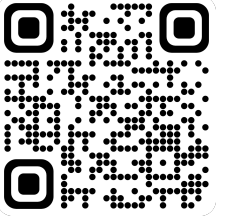
Input

An EOS E and an initial marking M .

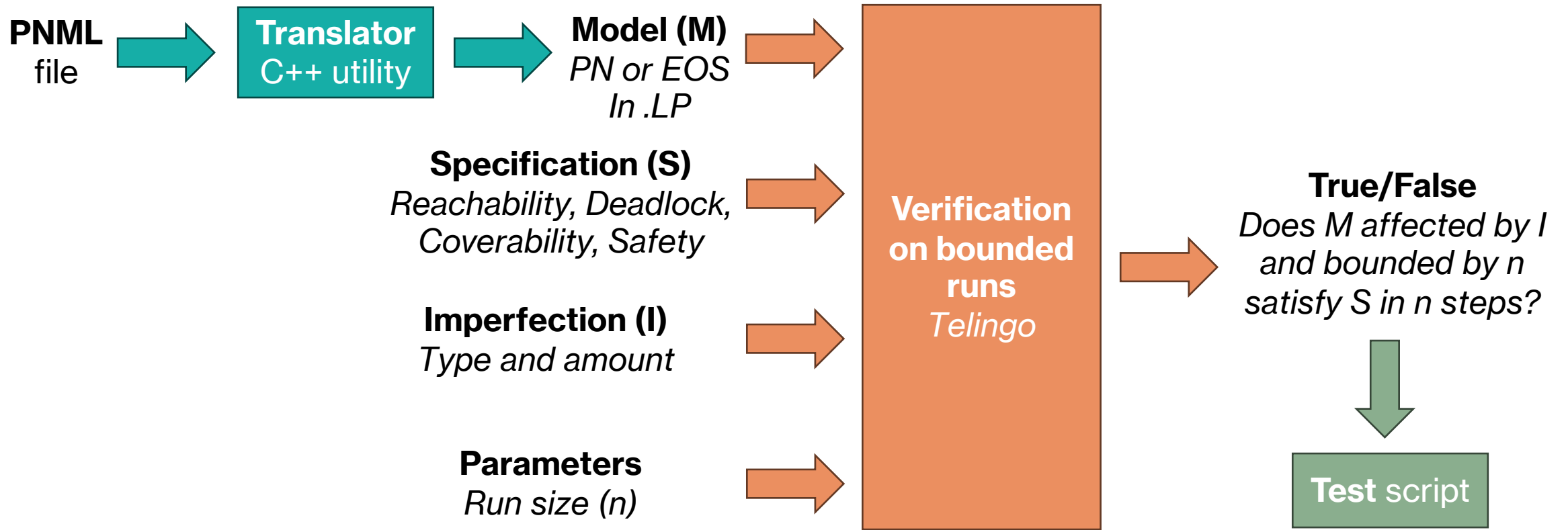
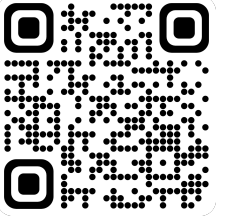
Output

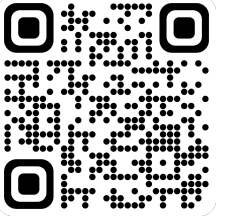
Is there a (\preceq, ℓ) -run from M to a marking where no event is enabled?

Motivation



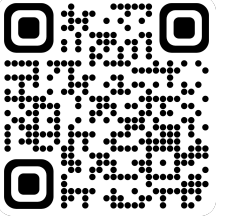
Prototype





Why bounded verification?

Problems on general EOS	\leq_f	\leq_o	\leq_s
0-reach	U	U	U
0-cover	U	U	U
ℓ -reach/cover	U	U	U
ω -reach/cover	D	U	U



Why Telingo?

Telingo is **declarative** and supports **temporal constraints**

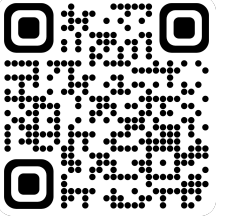
- E.g., `:- &tel(>? (lossy >(>? lossy))` allows at most one lossy step
- The meaning of lossy is declared orthogonally to EOS specification

Telingo **returns finite runs**

- Perfectly matches bounded verification

Encoding of PNs and EOSs is **elegant in ASP**

- E.g., when compared to SMT – R. Phawade, T. Prince, S. Sheerazuddin et al., *Bounded Model Checking for Unbounded Client Server Systems*, Arxiv (2022)



Correctness and performances

Correct answers

- Checked on MCC benchmarks

Slow on PNs

- Compared with Tapaal

Prohibitively slow on EOSs

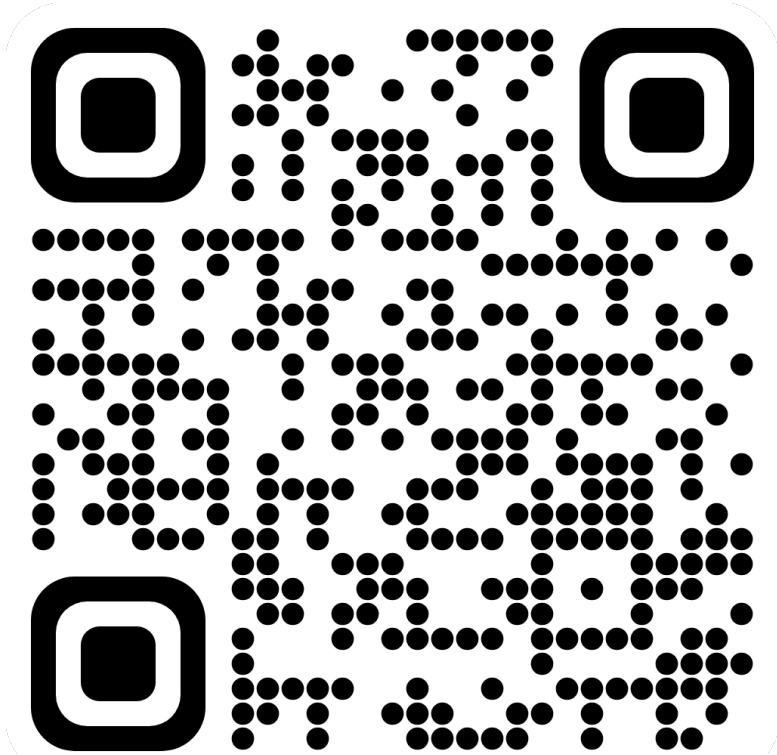
- Nesting exacerbates grounding

problem	lossiness	-imax =5 (s)	-imax =10 (s)	-imax =20 (s)	TAPAAL (s)
deadlock	none	UNSAT in 0.052	SAT in 0.622	SAT in 82.754	SAT in $5e - 6$
deadlock	any	SAT in 0.009	SAT in 0.010	SAT in 0.009	NA
1-safeness	none	UNSAT in 0.010	UNSAT in 0.014	UNSAT in 0.027	UNSAT in 0
1-safeness	any	UNSAT in 0.013	UNSAT in 0.018	UNSAT in 0.032	NA

Table 1

Comparative Results with TAPAAL for the Eratosthenes-PT-010 PN from the MCC benchmarks [12].

Give it a try



NWN Telingo Analyzer on Zenodo

*Translate PNs
from PNML to ASP*

*Analyze robustness
under lossiness*

Replicate our tests